



## Phase stability of (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites under low temperature hydrothermal conditions

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### Abstract

Y<sub>2</sub>O<sub>3</sub> and Nb<sub>2</sub>O<sub>5</sub> co-doped tetragonal zirconia polycrystals (TZP) containing 10 to 30 vol.% Al<sub>2</sub>O<sub>3</sub> ((Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub>) were sintered for 5 h at 1550°C in air and hydrothermal stability of the composites was evaluated after aging for 5 h at 180°C in 0.3 MPa H<sub>2</sub>O vapor pressure. (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites showed superior phase stability under the hydrothermal condition as compared with 3Y-TZP/Al<sub>2</sub>O<sub>3</sub> composites due to the effects of Y–Nb ordering in t-ZrO<sub>2</sub> and the Al<sub>2</sub>O<sub>3</sub> addition. The optimized strength and fracture toughness were 670 MPa and 7.3 MPa m<sup>1/2</sup>, respectively, when 20 vol.% of 2.8 μm Al<sub>2</sub>O<sub>3</sub> particles were added. © 1999 Elsevier Science B.V. All rights reserved.

**Keywords:** Tetragonal zirconia polycrystals; Y<sub>2</sub>O<sub>3</sub> and Nb<sub>2</sub>O<sub>5</sub> co-doped zirconia/Al<sub>2</sub>O<sub>3</sub> composite; Hydrothermal stability; Mechanical properties

### 1. Introduction

Although yttria-stabilized tetragonal zirconia polycrystals (Y-TZPs) possess high strength and toughness at room temperature, they suffer low-temperature strength degradation (LTD) because of the spontaneous tetragonal (t) to monoclinic (m) phase transformation when annealed at temperatures from 100 to 500°C in air. The LTD is accelerated under hydrothermal environments [1–3]. The phase stability of TZP under the hydrothermal conditions is a

critical requirement for applications of TZP for use in medical devices such as the femoral head in total hip replacement, dental implants, and scalpels. Attempts to alleviate LTD of Y-TZP through a decrease in grain size, an increase in yttrium content, and the formation of composites with Al<sub>2</sub>O<sub>3</sub> have been tried [3–8].

Considerable efforts have been exerted to elucidate the mechanism of hydrothermal degradation in Y-TZP. The yttrium depletion by Y(OH)<sub>3</sub> formation in the presence of water vapor by Lange et al. [2] was proposed as the cause of the aging-induced degradation. Yoshimura [9] suggested that the hy-

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drothermal degradation of Y-TZP is controlled by  $\text{OH}^-$  diffusion rather than  $\text{Y}(\text{OH})_3$  formation. Kim et al. [10–12] reported that LTD of Y-TZP is governed not by the existence of  $\text{H}_2\text{O}$  but the amount of residual stress in t- $\text{ZrO}_2$  during aging, which is accumulated by the diffusion of oxygen vacancies. The residual stress facilitates the t  $\rightarrow$  m phase transformation and the reaction between Zr–O–Zr bond and  $\text{H}_2\text{O}$ .

Recently, Lee et al. [13] examined the t-phase stability composition region in the  $\text{ZrO}_2$ – $\text{Y}_2\text{O}_3$ – $\text{Nb}_2\text{O}_5$  system and showed that  $\text{Nb}_2\text{O}_5$  doping to Y-TZP ((Y,Nb)-TZP) influenced remarkably the fracture toughness and LTD. The phase stability of TZPs in the ternary system is likely due to the Y–Nb ordering in t- $\text{ZrO}_2$  lattice [14]. The addition of  $\text{Al}_2\text{O}_3$  into Y-TZP enhanced fracture strength and phase stability because  $\text{Al}_2\text{O}_3$  particles acted as a grain-growth inhibitor for Y-TZP [15–17]. In particular, 2 to 3.85 mol% Y-TZP, alloyed with 20 to 40 wt.%  $\text{Al}_2\text{O}_3$  and prepared by hot isostatic pressing, exhibited extremely high strength of above 2 GPa [16], fracture toughness of 17 MPa  $\text{m}^{1/2}$  [15], and high temperature strength of 1 GPa at 1000°C [17]. Nevertheless, about 25% of t- $\text{ZrO}_2$  transformed to m- $\text{ZrO}_2$  during aging for 5 h at 180°C in an autoclave [18]. Although hydrothermal stability was improved by alloying with  $\text{CeO}_2$ , the (Y,Ce)-TZP/ $\text{Al}_2\text{O}_3$  composites exhibited about 10% of m- $\text{ZrO}_2$  after aging for 5 h at 180°C in hot water [18].

The objective of the present study is to investigate the hydrothermal stability of (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  composites containing 10 to 30 vol.% of  $\text{Al}_2\text{O}_3$  and to compare with that of 3Y-TZP/ $\text{Al}_2\text{O}_3$  composites after aging at 180°C for 5 h in an autoclave.

## 2. Experimental procedure

The powder preparation procedure of (Y,Nb)-TZP having a composition of 90.31 mol%  $\text{ZrO}_2$ —5.31 mol%  $\text{Y}_2\text{O}_3$ —4.45 mol%  $\text{Nb}_2\text{O}_5$  was reported elsewhere [13]. The starting powders, (Y,Nb)-TZP, 3Y-TZP (Tosoh, Japan), and  $\text{Al}_2\text{O}_3$  (Sumitomo Chemical, Japan) with different average particle sizes (0.2 and 2.8  $\mu\text{m}$ ), were ball milled for 24 h using zirconia balls. The amount of powders was measured on the basis of the theoretical densities of 6.02, 6.08,

and 3.99 for (Y,Nb)-TZP, 3Y-TZP, and  $\text{Al}_2\text{O}_3$ , respectively.  $\text{Al}_2\text{O}_3$  particles (0.2 and 2.8  $\mu\text{m}$ ) were mixed to (Y,Nb)-TZP and 3Y-TZP by 10 vol.% intervals in the range of 10 to 30 vol.%. The resulting composites are designated as YN10 $f(c)$ , YN20 $f(c)$ , YN30 $f(c)$ , 3Y10 $f(c)$ , 3Y20 $f(c)$ , and 3Y30 $f(c)$ , respectively. The last digit,  $f$  and  $c$ , indicates the  $\text{Al}_2\text{O}_3$  particle size, 0.2  $\mu\text{m}$  and 2.8  $\mu\text{m}$ , respectively.

The powders were uniaxially pressed into 34 mm  $\times$  34 mm  $\times$  5 mm rectangular plates at 98 MPa and then isostatically pressed at 138 MPa. The specimens were sintered at 1550°C with heating rates of 6°C/min to 900°C and 3°C/min up to the sintering temperature, and then furnace cooled to room temperature. The sintered specimens were ground and polished down to 1  $\mu\text{m}$  diamond finish.

The bulk density of (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  and 3Y-TZP/ $\text{Al}_2\text{O}_3$  composites was determined by the Archimedes method. The samples were aged for 1000 h at 250°C in air or for 5 h at 180°C in 0.3 MPa water vapor pressure in an autoclave. Phase stability of t- $\text{ZrO}_2$  after aging was studied using X-ray diffractometry. The proportion of the t and m-phase was estimated from the X-ray diffraction (XRD) peak heights of (111)<sub>m</sub>, (11-1)<sub>m</sub>, and (111)<sub>t</sub> after Garvie and Nicholson [19]. XRD patterns were obtained from the  $\text{CuK}\alpha$  radiation at 40 kV and 30 mA within the scan angles ( $2\theta$ ) of 27° to 35°. The linear intercept method was used to determine the average grain size with the use of a correction factor of 1.56 after Mendelson [20].

The rectangular specimens were ground and cut with diamond saw to a size of 24 mm  $\times$  4 mm  $\times$  3 mm, and subsequently annealed for 1 h at 1200°C. The flexural strength was measured using a 3-point bending with a 20 mm outer span at a crosshead speed (Instron 4204) of 0.5 mm/min. Fracture toughness of bar specimens was then assessed using the indentation/strength method [21]. A Vickers indent of 294 N was placed on the center of the tensile face of each test piece by aligning the pyramidal edges to the longitudinal axis for the bar specimens. To prevent the stress-corrosion cracking, a silicon oil was dropped on the indented site and then specimens were broken using a 4-point bending fixture. The hardness-to-modulus ratio ( $H/E$ ) was determined by measuring the dimensions of the Knoop indentation

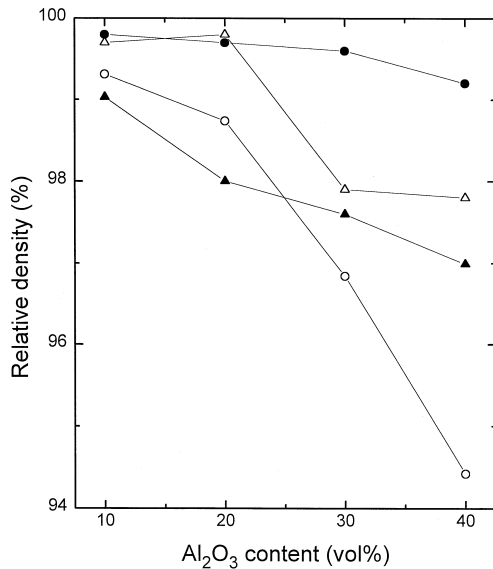


Fig. 1. Relative density of 3Y-TZP/ $\text{Al}_2\text{O}_3$  and (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  composites having different  $\text{Al}_2\text{O}_3$  particle sizes, where the specimens were sintered for 5 h at  $1550^\circ\text{C}$  in air. ● (Y,Nb)-TZP/ $2.8\ \mu\text{m}\ \text{Al}_2\text{O}_3$ ; ▲ (Y,Nb)-TZP/ $0.2\ \mu\text{m}\ \text{Al}_2\text{O}_3$ ; ○ 3Y-TZP/ $2.8\ \mu\text{m}\ \text{Al}_2\text{O}_3$ ; △ 3Y-TZP/ $0.2\ \mu\text{m}\ \text{Al}_2\text{O}_3$ .

impression dimensions as reported by Marshall et al. [22].

### 3. Results and discussion

The relative density of the composites, sintered for 5 h at  $1550^\circ\text{C}$  in air, is shown in Fig. 1. The relative density of YN10c rose from 97.8% to 99.8% as the sintering time increased from 1 h to 5 h. This is consistent with the densification behavior of 3Y-TZP/ $\text{Al}_2\text{O}_3$  reported by Upadhyaya et al. [23]. The relative density of all composites decreased as the content of  $\text{Al}_2\text{O}_3$  increased from 10 to 40%. The reduction in the density may be ascribed to a reduced grain boundary mobility of the zirconia matrix with

increasing ratio of  $\text{Al}_2\text{O}_3$  reinforcement as a result of limited interdiffusion caused by an increase in the diffusion path lengths [23].

The grain size and m- $\text{ZrO}_2$  content of 3Y-TZP and (Y,Nb)-TZP are summarized in Table 1. All specimens showed t- $\text{ZrO}_2$  phase only after sintering for 5 h at  $1550^\circ\text{C}$  in air. When 3Y-TZP was annealed for 1000 h at  $250^\circ\text{C}$  in air, XRD results revealed that about 65% of the t- $\text{ZrO}_2$  phase transformed to m- $\text{ZrO}_2$  even though the grain size of 3Y-TZP,  $0.7\ \mu\text{m}$ , was much smaller than that of (Y,Nb)-TZP shown in Table 1. The beneficial effect of the  $\text{Nb}_2\text{O}_5$  alloying into Y-TZP on its aging resistance is clearly seen from Table 1 where no m- $\text{ZrO}_2$  phase was observed on (Y,Nb)-TZP after aging in air or in an autoclave. The absence of the degradation in (Y,Nb)-TZP under the low-temperature conditions is attributed to local Y-Nb ordering in t- $\text{ZrO}_2$  into a scheelite-like arrangement [13,14], which results in a relief of the internal strain in the t- $\text{ZrO}_2$  lattice since the internal stress causes the degradation [10–12]. Furthermore, the concentration of oxygen vacancy in t- $\text{ZrO}_2$ , created by the  $\text{Y}^{3+}$  doping, decreased by the addition of  $\text{Nb}^{5+}$ , leading to a low vacancy diffusion rate which governed the t  $\rightarrow$  m phase transformation during aging at low temperatures [11,12].

After aging in air and in water vapor, XRD analysis of the aged composites showed that the amount of m- $\text{ZrO}_2$  decreased with increasing  $\text{Al}_2\text{O}_3$  content, as shown in Fig. 2. The decrease in m- $\text{ZrO}_2$  by the addition of  $\text{Al}_2\text{O}_3$  is likely achieved by hindering a relaxation of the strained t- $\text{ZrO}_2$  lattice due to the presence of the rigid  $\text{Al}_2\text{O}_3$  particles. The m- $\text{ZrO}_2$  content of 3Y10f was 24% after aging in air. The degree of t  $\rightarrow$  m phase transformation increased significantly from 24% to 70% when 3Y10f was exposed to aging in the autoclave since the high pressure aging condition accelerates the relaxation [11]. The addition of  $2.8\ \mu\text{m}\ \text{Al}_2\text{O}_3$  into 3Y-TZP raised the amount of m- $\text{ZrO}_2$  almost close to 3Y-TZP

Table 1

Grain size and m- $\text{ZrO}_2$  content of 3Y-TZP and (Y,Nb)-TZP sintered for 5 h at  $1550^\circ\text{C}$  in air

Sample	Grain size ( $\mu\text{m}$ )	m- $\text{ZrO}_2$ (%), aging in air	m- $\text{ZrO}_2$ (%), aging in autoclave
3Y-TZP	0.7	65	87
(Y,Nb)-TZP	2.4	0	0

Specimens are aged for 1000 h at  $250^\circ\text{C}$  in air or for 5 h at  $180^\circ\text{C}$  in 0.3 MPa water vapor pressure.

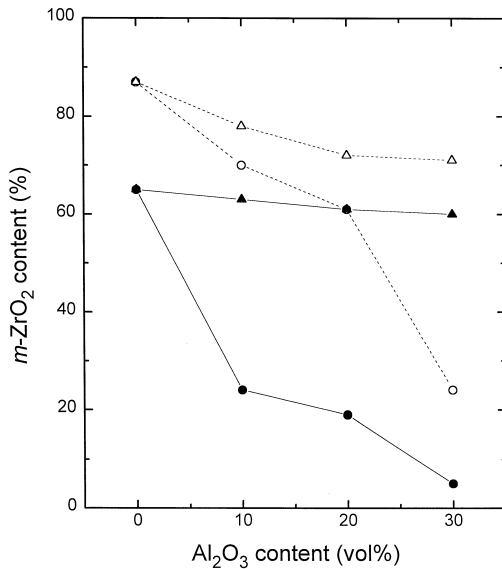


Fig. 2. Fraction of *m*-ZrO<sub>2</sub> of the aged surfaces of 3Y-TZP/Al<sub>2</sub>O<sub>3</sub> and (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites as a function of Al<sub>2</sub>O<sub>3</sub> content, where the specimens were sintered at 1550°C for 5 h and aging was performed for 1000 h at 250°C in air or for 5 h at 180°C in 0.3 MPa H<sub>2</sub>O vapor pressure. ● 3Y-TZP/0.2 μm Al<sub>2</sub>O<sub>3</sub> in air; ▲ 3Y-TZP/2.8 μm Al<sub>2</sub>O<sub>3</sub> in air; ○ 3Y-TZP/0.2 μm Al<sub>2</sub>O<sub>3</sub> in autoclave; △ 3Y-TZP/2.8 μm Al<sub>2</sub>O<sub>3</sub> in autoclave.

after aging as shown in Fig. 2, indicating that the larger Al<sub>2</sub>O<sub>3</sub> particles were little influential in the phase stability of the composites probably due to the large grain size. In contrast, there was no degradation in (Y,Nb)-TZP regardless of the Al<sub>2</sub>O<sub>3</sub> content owing to the inherent phase stability of t-ZrO<sub>2</sub> in this composition [13].

Flexural strength and fracture toughness of (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites containing 0 to 30 vol.% Al<sub>2</sub>O<sub>3</sub> are shown in Fig. 3. The flexural strength of (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites increased as Al<sub>2</sub>O<sub>3</sub> was added up to 20 vol.% and then decreased with further addition of Al<sub>2</sub>O<sub>3</sub>, which is consistent with the results reported earlier [16,23,24]. This reduction in strength above 20 vol.% of Al<sub>2</sub>O<sub>3</sub> may be explained by decrease in constraint on the t-ZrO<sub>2</sub> as a result of the low bulk density [24]. Although flexural strength of YN20*f* was slightly higher than that of YN20*c*, the optimized strength and fracture toughness, 670 MPa and 7.3 MPa m<sup>1/2</sup>, were observed when 20 vol.% of 2.8 μm Al<sub>2</sub>O<sub>3</sub> particles were added. SEM micrographs of (Y,Nb)-

TZP/Al<sub>2</sub>O<sub>3</sub> composites containing 10 to 30 vol.% of 2.8 μm Al<sub>2</sub>O<sub>3</sub> are shown in Fig. 4. The white and the black grains indicate ZrO<sub>2</sub> grains and Al<sub>2</sub>O<sub>3</sub> grains, respectively. The grain size of ZrO<sub>2</sub> in the (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites was smaller than that in monolithic (Y,Nb)-TZP [13], indicating the role of Al<sub>2</sub>O<sub>3</sub> as a grain growth inhibitor.

XRD results of the fracture surfaces of (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> and 3Y-TZP/Al<sub>2</sub>O<sub>3</sub> composites are shown in Fig. 5 as a function of Al<sub>2</sub>O<sub>3</sub> content. In both composites, the fraction of *m*-ZrO<sub>2</sub> decreased with increasing the amounts of Al<sub>2</sub>O<sub>3</sub>. However, the decreasing rate of *m*-ZrO<sub>2</sub> in the composites having 0.2 μm Al<sub>2</sub>O<sub>3</sub> particles is more pronounced compared with that in the composites having 2.8 μm Al<sub>2</sub>O<sub>3</sub> particles, indicating that the influence of the stress-induced phase transformation on mechanical properties of the composites is lessened with increased Al<sub>2</sub>O<sub>3</sub> contents and decreased Al<sub>2</sub>O<sub>3</sub> particle size due to the decrease in transformable t-ZrO<sub>2</sub> content. Nevertheless, (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites showed the optimized fracture toughness of 7.3 MPa m<sup>1/2</sup> and 6.4 MPa m<sup>1/2</sup>, respectively, when 20

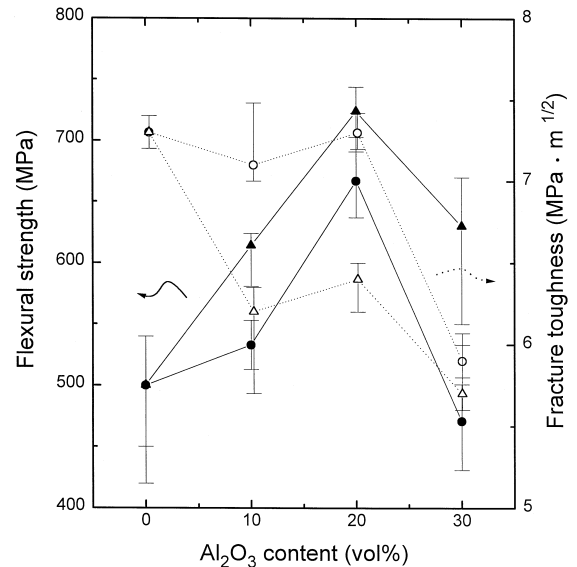


Fig. 3. Flexural strength and fracture toughness of (Y,Nb)-TZP/Al<sub>2</sub>O<sub>3</sub> composites, prepared by sintering for 5 h at 1550°C in air, as a function of Al<sub>2</sub>O<sub>3</sub> content. ● (Y,Nb)-TZP/2.8 μm Al<sub>2</sub>O<sub>3</sub>; ▲ (Y,Nb)-TZP/0.2 μm Al<sub>2</sub>O<sub>3</sub>; ○ (Y,Nb)-TZP/2.8 μm Al<sub>2</sub>O<sub>3</sub>; △ (Y,Nb)-TZP/0.2 μm Al<sub>2</sub>O<sub>3</sub>.

vol.% of 2.8  $\mu\text{m}$  and 0.2  $\mu\text{m}$   $\text{Al}_2\text{O}_3$  particles were added, as shown in Fig. 3. The highest fracture

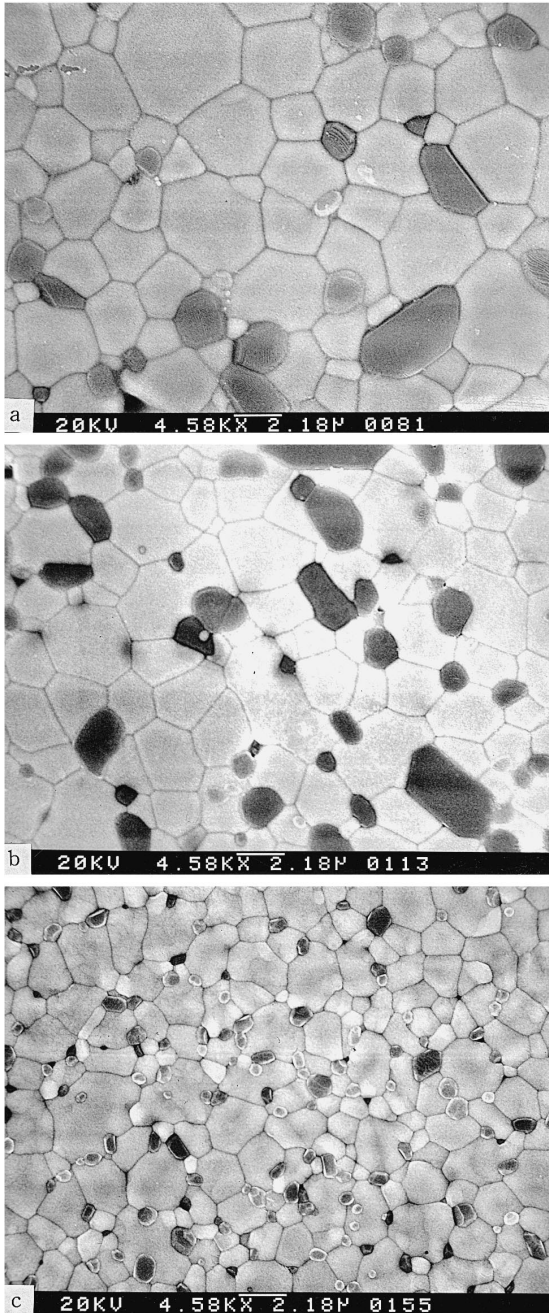


Fig. 4. Scanning electron micrographs of the thermally etched surface of (Y,Nb)-TZP/2.8  $\mu\text{m}$   $\text{Al}_2\text{O}_3$  composites after sintering for 5 h at 1550°C in air. (a) 10 vol.% of  $\text{Al}_2\text{O}_3$ ; (b) 20 vol.%; (c) 30 vol.%.

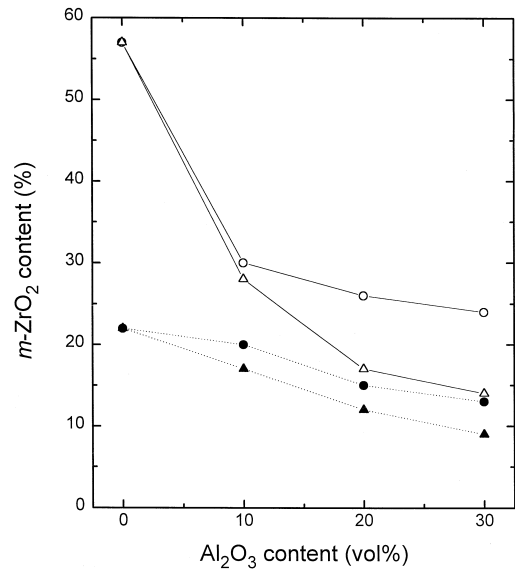


Fig. 5. Fraction of m-ZrO<sub>2</sub> on the fracture surfaces of 3Y-TZP/ $\text{Al}_2\text{O}_3$  and (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  composites, sintered at 1550°C for 5 h in air, as a function of  $\text{Al}_2\text{O}_3$  content. ● 3Y-TZP/2.8  $\mu\text{m}$   $\text{Al}_2\text{O}_3$ ; ▲ 3Y-TZP/0.2  $\mu\text{m}$   $\text{Al}_2\text{O}_3$ ; ○ (Y,Nb)-TZP/2.8  $\mu\text{m}$   $\text{Al}_2\text{O}_3$ ; △ (Y,Nb)-TZP/0.2  $\mu\text{m}$   $\text{Al}_2\text{O}_3$ .

toughness at these composition indicates that the fracture toughness strongly depends on the strength according to the Griffith relationship [25]. And the toughness difference between YN20c and YN20f may be ascribed to the contribution of transformation toughening and the grain bridging due to the  $\text{Al}_2\text{O}_3$  particle size [26]. Therefore, the  $\text{Al}_2\text{O}_3$  particle with larger size was more effective to increase fracture toughness of the composites with the same  $\text{Al}_2\text{O}_3$  content.

#### 4. Conclusions

No hydrothermal degradation was observed on (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  composites after aging for 5 h at 180°C and 0.3 MPa in an autoclave, however, extensive t  $\rightarrow$  m phase transformation was found in 3Y-TZP/ $\text{Al}_2\text{O}_3$  composites. The m-ZrO<sub>2</sub> content of the aged 3Y-TZP/ $\text{Al}_2\text{O}_3$  composites decreased with increasing  $\text{Al}_2\text{O}_3$  content due to the stability of t-ZrO<sub>2</sub> caused by the addition of  $\text{Al}_2\text{O}_3$ . Therefore, the Nb<sub>2</sub>O<sub>5</sub> doping to Y-TZP is more effective to the phase stability than  $\text{Al}_2\text{O}_3$  alloying into Y-TZP.

The optimized strength and fracture toughness of (Y,Nb)-TZP/ $\text{Al}_2\text{O}_3$  composite, sintered for 5 h at  $1550^\circ\text{C}$  in air, were 670 MPa and  $7.3 \text{ MPa m}^{1/2}$ , respectively when 20 vol.% of  $2.8 \mu\text{m}$   $\text{Al}_2\text{O}_3$  was added. Fracture toughness increase was better in the composite dispersed with  $\text{Al}_2\text{O}_3$  particle of larger size.

## References

- [1] T. Sato, M. Shimada, *J. Am. Ceram. Soc.* 68 (6) (1985) 356.
- [2] F.F. Lange, G.L. Dunlop, B.I. Davis, *J. Am. Ceram. Soc.* 69 (3) (1986) 237.
- [3] S. Lawson, *J. Eur. Ceram. Soc.* 15 (1995) 485.
- [4] S.Y. Chen, H.Y. Lu, *J. Mater. Sci.* 23 (1988) 1195.
- [5] D. Basu, A. Das Gupta, M.K. Basu, B.K. Sarkar, *J. Eur. Ceram. Soc.* 16 (1996) 613.
- [6] M.M.R. Boutz, A.J.A. Winnubst, B. Van Langerak, R.J.M. Olde Scholtenhuis, K. Kreuwel, A.J. Burggraaf, *J. Mater. Sci.* 30 (1995) 1854.
- [7] A.E. Hughes, H. St. John, P. Koutouros, H. Schubert, *J. Eur. Ceram. Soc.* 15 (1995) 1125.
- [8] M.T. Hernandez, J.R. Jurado, P. Duran, J.L.G. Fierro, *J. Am. Ceram. Soc.* 74 (1991) 1254.
- [9] M. Yoshimura, *Am. Ceram. Soc. Bull.* 67 (12) (1988) 1950.
- [10] D.-J. Kim, H.-J. Jung, D.-H. Cho, *Solid State Ionics* 80 (1995) 67.
- [11] D.-J. Kim, *J. Eur. Ceram. Soc.* 17 (1997) 897.
- [12] D.-J. Kim, H.-J. Jung, J.-W. Jang, H.-L. Lee, *J. Am. Ceram. Soc.*, in press.
- [13] D.Y. Lee, D.-J. Kim, D.-H. Cho, *J. Mater. Sci. Lett.* 17 (1998) 185.
- [14] P. Li, I.-W. Chen, J.E. Penner-Hahn, *J. Am. Ceram. Soc.* 77 (1994) 1289.
- [15] J. Li, R. Watanabe, *J. Am. Ceram. Soc.* 78 (1995) 1079.
- [16] K. Tsukuma, K. Ueda, M. Shimada, *J. Am. Ceram. Soc.* 68 (1985) C4.
- [17] K. Tsukuma, K. Ueda, K. Matsushita, M. Shimada, *J. Am. Ceram. Soc.* 68 (1985) C56.
- [18] M. Hirano, H. Inada, *J. Ceram. Soc. Jpn.* 99 (1991) 124.
- [19] R.C. Garvie, P.S. Nicholson, *J. Am. Ceram. Soc.* 55 (1972) 303.
- [20] M.J. Mendelson, *J. Am. Ceram. Soc.* 52 (1969) 443.
- [21] P. Chantikul, G.R. Anstis, B.R. Lawn, D.B. Marshall, *J. Am. Ceram. Soc.* 64 (1981) 539.
- [22] D.B. Marshall, T. Noma, A.G. Evans, *Commun. Am. Ceram. Soc.* 65 (1982) C-175.
- [23] D.D. Upadhyaya, P.Y. Lalvi, G.K. Dey, *J. Mater. Sci.* 28 (1993) 6103.
- [24] J.L. Shi, B.S. Li, T.S. Yen, *J. Mater. Sci.* 28 (1993) 4019.
- [25] B. Lawn, *Fracture of Brittle Solids*, 2nd ed. Cambridge Univ. Press, Cambridge, UK, 1993.
- [26] D.Y. Lee, D.-J. Kim, *J. Am. Ceram. Soc.*, to be submitted.